# Analysis on Relationship Between Signal Intensity and Antenna Height of Localizer Antenna Array by Digital Twin 

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#### Abstract

To obtain optimized space radiation signal to satisfy the coverage requirement, it is essential to set the height of radiated antenna ( $h_{a}$ ) effectively. Theoretical analysis with a series $h_{a}$ (from 1 m to 20 m ) of mirror signal synthesis was studied. The three-dimensional mathematical model of localizer antenna array of 7216A was also established. Because of synthesis lobe effect, the variety of $h_{a}$ can adjust the signal strength in vertical. The radio frequency (RF) level would increase obviously with ascending of $h_{a}$. This phenomenon presents extremely regularly in low altitude. Two curve surface models, conical surface and contour plane, with a series of height of antenna ( $h_{a}=1 \mathrm{~m}, 2 \mathrm{~m}, 3 \mathrm{~m}, 4 \mathrm{~m}, 5 \mathrm{~m}, 10 \mathrm{~m}, 15 \mathrm{~m}, 20 \mathrm{~m}$ ) and three fly height $\left(\mathrm{h}_{\mathrm{fly}}=\right.$ $100 \mathrm{~m}, 600 \mathrm{~m}, 3000 \mathrm{~m}$ ) were analyzed. With the excessively increasing of $h_{\mathrm{a}}$, however, RF value would fluctuate in large elevation. At the same time, headspace blind area combines with circle effect become obvious. The study showed $h_{a}$ rose to 4 meter presents a good quality. This result fits for any localizer antenna array of Instrument Landing System (ILS).


Keywords: mirror signal synthesis, horizontal polarization, signal strength, antenna height

## 1. Introduction

Localizer antenna array is horizontal polarization. After radiated signal reflected from ground, the synthesis signal combined with direct one and reflected one generates the lobe(s) oblique upward. This main synthetic lobe provides approach and landing guidance ${ }^{[1]}$ for aeroplanes. The types of localizer beacon are the most abundant in Instrument Landing System (ILS) equipment. According to actual needs, they came out one after another. Such as series the early 3500 -series: $3522^{[2]}, 3523 B^{[3]}, 3524^{[4]}, 3525^{[5]}, 3526^{[6]}$ and the later 7000 -series: $7212 \mathrm{~A}^{[7]}, 7212 \mathrm{C}^{[8]}, 7216 \mathrm{~A}^{[9]}, 7216 \mathrm{C}^{[10]}, 7220 \mathrm{~A}^{[11]}, 7220 \mathrm{~B}^{[12]}$ were produced by Normarc factory; and single frequency: 8 -unit moderate-aperture, 12 -unit medium-aperture, dual frequency: 13 -unit wideaperture, 21 -unit ultrawide-aperture ${ }^{[133]}$, and 420-series: 14 -unit, 20 -unit manufactured by Thales company; dual frequency:14-unit, 16 -unit, 20 -unit were designed one after another by Selex ${ }^{[14]}$ company. The series above are mainly distinguished by horizontal radiated pattern. They almost play the same role in vertical pattern. However, the vertical pattern depends on the elevation $\left(\theta_{v}\right)$ changing of the main lobe. And the elevation is directly controlled by $\mathrm{h}_{\mathrm{a}}$. Correct setting of $\theta_{\mathrm{v}}$ can improve intensity effectively of signal coverage. At the same time, optimized $h_{a}$ would provide more energy-saving environment and longer lifecycle of localizer equipment in further operation. Otherwise, incorrect installation may cause insufficient coverage distance.

In this paper, $\mathrm{h}_{\mathrm{a}}$ corresponding to the intensity of localizer was studied. This result fits to all the kind of localizer antenna array. The 3D mathematical model of 7216A localizer system was established. Two surface coverage models and radiated electromagnetic signal distribution of localizer array were simulated by software Matrix Laboratory (Matlab).

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## 2. Result and Discussion

### 2.1. Relationship Between $H_{a}$ and Signal Distribution

### 2.1.1. Mirror Signal Synthesis

There are two components contributes to localizer signal in space. The direct radiated signal and its reflected signal. Two signals overlay in space. the amplitude of two signals is regarded as approximately the same. This signal superposition mode is called mirror signal synthesis.

In general, there are two kind of polarization modes, horizonal polarization and vertical polarization. They are widely used in radio field. The basic principle of polarization formation was introduced in figure 1 , a charged metal rod $A B$ and its reflected one marked $c$, they have the same distance (h) from the reflecting surface. When the rod positioned parallel to reflecting surface, it words as horizontal polarization. The phase of the reflected signal ( $\mathrm{A}^{\prime} \mathrm{B}^{\prime}$ ) is opposite to the direct signal ( AB ). When the rod positioned perpendicular to reflecting surface, rod $A B$ works as vertical polarization. The phase of the reflected signal is same to direct one.

Localizer antenna array consists of a row of Log Periodic Dipole Antenna (LPDA). They are placed parallel to ground, so polarization mode is horizontal polarization. The reflected signal owns the opposite phase.


Fig.1: Electronic polarization formation.
Terminal A is positive of charged metal rod while another terminal $B$ is negative. Through reflection the mirror rod, terminal A' becomes negative and terminal B' turns to positive. There are two polarization method, horizontal polarization and vertical polarization. The black dot is the center of the rod AB , the height from the reflector is h . The gray dot is the center of the mirror symmetry rod A'B'. If the angle $(\theta)$ is $0^{\circ}$, namely metal rod parallel with reflector, $\operatorname{rod} \mathrm{AB}$ is horizontal polarization. The reflected signal owns the opposite phase to original one, If the angle $(\theta)$ is $90^{\circ}$, namely charged metal rod perpendicular to reflector, rod AB is vertical polarization. Both the original and reflected one own identical phase.

### 2.1.2. Relationship Between $H_{a}$ and Lobe

Mirror signal synthesis generates directional lobes. Direct signal and reflected signal with identical amplitude but opposite phase overlay in space. Because of phase difference of two signal in space, synthetic signal is not omnidirectional distribution any more. It can be seen in figure 2 , no matter how high $h$, there is little signal in horizontal plane $\left(\theta_{\mathrm{v}}=0^{\circ}\right)$. A series of lobes appear with the ascending of $h_{\mathrm{a}}$. there is a rule that the number of lobes in every quadrant is proportional to h in electrical length. Quantitively speaking, every half of wavelength contributes a whole lobe in every quadrant. If $h$ is less than half of wavelength, still one lobe is first quadrant existing, and mirror symmetry in each quadrant.




$\mathrm{h}=1.25 \lambda$


Fig.2: Opposite phase synthesis with different electrical length.
The gap (h) between original dot (black one) and reflector should be transferred to electrical length. Every half of lambda contributes a whole lobe in every quadrant. While h is 1.5 times of wavelength, there are three lobes generated in the first quadrant. It can be inferred that if h was 2 times of wavelength, there were four lobes generated. The number of synthesis lobe increasing with the extending of electrical length. The amplitude of synthesis lobe is always zero at the position $\theta_{\mathrm{v}}=0^{\circ}$.

### 2.1.3. Vertical Signal of Log Periodic Dipole Antenna on Ground

The frequency ( f ) of localizer system is taken 110.1 MHz , then the corresponding wavelength ( $\lambda$ ) is 2.72 m. Only the first quadrant should be considered in application. A series of $h_{a}$ corresponding to vertical pattern was exhibited in figure 3. In the center of the figure, the vertical radiated pattern of LPDA was listed. It is just like the case of no actual height ( $h_{a}=0 \mathrm{~m}$ ). Once $h_{a}$ exists, no matter how less, signal strength disappears immediately at $\theta_{\mathrm{v}}=0^{\circ}$. The synthesis signal becomes upturned lobe. For the case of $\mathrm{h}_{\mathrm{a}}=1 \mathrm{~m}$, the wavelength is less than half of $\lambda(\lambda / 2=1.36 \mathrm{~m})$, only one lobe appears. When $\mathrm{h}_{\mathrm{a}}$ arrives at 2 m , the corresponding electronic length is about $0.73 \lambda$, which is more than $0.5 \lambda$, two lobes appear. The number of the lobes are increasing monotony with the ascending of $h_{a}$.

Different to the case in figure 2, the amplitude of every lobes listed in figure3 are not equal. This phenomenon attributes to the vertical pattern of LPDA, which is not omnidirectional, the maximum value ( $\mathrm{E}_{\text {max }}$ ) is located in the position of $\theta_{\mathrm{v}}=0^{\circ}$. The amplitude attenuates with the increasing of $\theta_{\mathrm{v}}$. It can be found in the center of the figure, the vertical pattern of LPDA, the half power point is $\theta_{\mathrm{v}}=33^{\circ}$. So, the first lobe owns the maximum amplitude always.


Fig.3: Vertical radiated pattern of LPDA corresponding to $h_{\mathrm{a}}$.

The frequency (f) of localizer signal is taken 110.1 MHz , then the corresponding wavelength ( $\lambda$ ) is 2.72 m . When the height of antenna is 1 m , there are 0.36 times of $\lambda$, there is only one lobe appears. When the height of antenna is 2 m , there are 0.73 times of $\lambda$, namely more than 0.5 times of $\lambda$, there are more than one lobe generated. The lobes appear in positive proportion to $h_{a}$. While $h_{a}=0$, the synthesis formation is the vertical pattern of LPDA, listed in the center of the figure.

### 2.2. Relationship Between $\mathrm{H}_{\mathrm{a}}$ and Receive Position

In this section, according to the distribution of 7216A antenna array, signal strength radiated at specific receive point in space would be discussed.

### 2.2.1 Signal Characteristic at Different Azimuth

The 7216A antenna array consists of sixteen elements, the mirror symmetry from center generates eight pairs ${ }^{[9]}$. The width of the antenna array is 38.5 m . The total horizontal pattern of sixteen LPDAs can be found figure 4, there is a sharp lobe right ahead. This sharp lobe is divided equally by the runway centerline. The azimuth located in centerline is defined as $\theta_{\mathrm{h}}=0^{\circ}$.

The horizonal pattern of one single LPDA is marked at the right top of the figure. The specific step to establish the field signal can refer to reference 15 . According to horizontal pattern, five points with radius of 1 km are chosen to be analyzed. Namely $\theta_{\mathrm{h}}=-35^{\circ},-10^{\circ}, 0^{\circ},+10^{\circ},+35^{\circ}$. All the height of these points is 10 m . The position in front of the center of antenna with a distance of $\mathrm{r}_{2}=5 \mathrm{~km}$ is also calculated in the discussion below.


Fig.4: Horizontal radiated pattern of LPDA and 7216A localizer antenna array.
Inset shows the horizontal pattern of single LPDA. 7216A localizer antenna array consists of sixteen LPDAs, the total width of the array is 38.5 m . Both LPDA and antenna array compose the whole horizontal pattern. There are two radiuses taken into consider, $\mathrm{r}_{1}=1 \mathrm{~km}$ and $\mathrm{r}_{2}=5 \mathrm{~km}$. There are five point chosen for $\mathrm{r}_{1}=1 \mathrm{~km}$, azimuth $\left(\theta_{\mathrm{h}}\right)$ from $-35^{\circ}$ to $+35^{\circ}$, namely $\theta_{\mathrm{h}}=-35^{\circ},-10^{\circ}, 0^{\circ},+10^{\circ},+35^{\circ}$.

From five points with radius of $\mathrm{r}_{1}=1 \mathrm{~km}$ and 10 m high, the RF corresponding to $\mathrm{h}_{\mathrm{a}}$ has been calculated, exhibited in figure 5 . RF level of each point increases monotonically with the increasing of $\mathrm{h}_{\mathrm{a}}$. The value of $\theta_{\mathrm{h}}=0^{\circ}$ is maximum, second for $\theta_{\mathrm{h}}= \pm 10^{\circ}$ and minimum for $\theta_{\mathrm{h}}= \pm 35^{\circ}$. Although RF is rising with ascending of $h_{a}$, it is not increasing linearly. The increment ( $\Delta R F$ ) is getting smaller and smaller in high region of $h_{a}$. It is not advisable to increase $h_{a}$ blindly. The fitting curve indicates the critical point $\left(h_{c}\right)$ of $h_{a}$ corresponding curve. When $h_{a}$ below $h_{c}$, the increment is obvious, but once $h_{a}$ above this value, the increment of RF would not be effective any more.


Fig.5: RF level corresponding to $h_{a}$ in different azimuth.
All the data tested 10 -meter-high ( $h_{\text {fly }}=10 \mathrm{~m}$ ). Fitted curve shows the critical point at $h_{\mathrm{c}}=4 \mathrm{~m}$. RF level increases with the ascending of $h_{a}$, it grows quickly in low $h_{a}$ zone, when $h_{a}$ is higher than $4 m$, the growth becomes much slower.

The increment of RF ( $\Delta \mathrm{RF}$ ) is calculated quantitatively for two ways. Table 1 lists the $\Delta R F$ by ascending one meter of $h_{a}$. For example, when $h_{a}=1 \mathrm{~m}$ is elevated to $h_{a}=2 m$, the corresponding increment of RF is 6 dBm . When $h_{\mathrm{a}}$ is elevated from 2 m to $3 \mathrm{~m}, \Delta \mathrm{RF}$ turns to 3.5 dBm for $\theta_{\mathrm{h}}=0^{\circ}$ and 3.6 dBm for $\theta_{\mathrm{h}}=$ $\pm 10^{\circ}$ and $\theta_{\mathrm{h}}= \pm 35^{\circ}$. When $h_{\mathrm{a}}$ is below 4 m , the increment of RF is more than 2 dBm . When $h_{a}$ is higher than 8 m , corresponding $\Delta \mathrm{RF}$ is less than 1 dBm . So, if you want to improve $R F$ level by ascending $h_{a}$ linearly, $h_{c}=4 \mathrm{~m}$ is critical transition height.

Table 1: Increment of RF ( $\Delta \mathrm{RF}$ ) for ascending $\Delta \mathrm{h}_{\mathrm{a}}=1 \mathrm{~m}$

| $\mathrm{h}_{\mathrm{a}}(\mathrm{m})$ | $0^{\circ}(\mathrm{dBm})$ | $10^{\circ}(\mathrm{dBm})$ | $35^{\circ}(\mathrm{dBm})$ |
| :---: | :---: | :---: | :---: |
| $1 \rightarrow 2$ | 6.0 | 6.0 | 6.0 |
| $2 \rightarrow 3$ | 3.5 | 3.6 | 3.6 |
| $3 \rightarrow 4$ | 2.5 | 2.5 | 2.4 |
| $4 \rightarrow 5$ | 2.0 | 1.9 | 2.0 |
| $5 \rightarrow 6$ | 1.5 | 1.6 | 1.6 |
| $6 \rightarrow 7$ | 1.4 | 1.3 | 1.3 |
| $7 \rightarrow 8$ | 1.1 | 1.1 | 1.1 |
| $8 \rightarrow 9$ | 1.0 | 1.0 | 1.0 |
| $9 \rightarrow 10$ | 1.0 | 0.9 | 0.9 |
| $10 \rightarrow 11$ | 0.7 | 0.8 | 0.9 |

The other way to improve RF level is ascending $h_{a}$ by doubling, seen the calculation result in table 2. When $h_{a}$ is doubled, the increment is almost approximately 6.0 dBm . When $h_{a}$ has been reached a high value, the increment of RF needs significant improvement of $h_{\mathrm{a}}$. In other words, if the RF level need be enhanced by certain decibels, the $h_{a}$ should be doubled.

Table 2: Increment of RF ( $\Delta \mathrm{RF}$ ) for double $\mathrm{h}_{\mathrm{a}}$

| $\mathrm{h}_{\mathrm{a}}(\mathrm{m})$ | $0^{\circ}(\mathrm{dBm})$ | $10^{\circ}(\mathrm{dBm})$ | $35^{\circ}(\mathrm{dBm})$ |
| :---: | :---: | :---: | :---: |
| $1 \rightarrow 2$ | 6.0 | 6.0 | 6.0 |
| $2 \rightarrow 4$ | 6.0 | 6.1 | 6.0 |
| $3 \rightarrow 6$ | 6.0 | 6.0 | 6.0 |
| $4 \rightarrow 8$ | 6.0 | 5.9 | 6.0 |
| $5 \rightarrow 10$ | 6.0 | 5.9 | 5.9 |
| $6 \rightarrow 12$ | 6.0 | 5.9 | 5.9 |
| $7 \rightarrow 14$ | 6.0 | 5.9 | 5.9 |
| $8 \rightarrow 16$ | 5.9 | 5.9 | 5.9 |
| $9 \rightarrow 18$ | 5.9 | 5.9 | 5.9 |
| $10 \rightarrow 20$ | 5.9 | 5.8 | 5.8 |

There is a little difference of $\Delta R F$ of three azimuths in both tables. This is contributed to near field characteristic. The signal in far field would trend to the same of different azimuths. The variation of RF by changing $h_{a}$ of far field model could be described as formula 1 :

$$
\Delta R F=20 \log \frac{\sin \left(\frac{2 \pi}{\lambda} h_{a}^{\prime} \sin \theta_{v}\right)}{\sin \left(\frac{2 \pi}{\lambda} h_{a} \sin \theta_{v}\right)}
$$

When the height is far less than horizontal distance, $\theta_{\mathrm{v}}$ is negligible, $\sin \left(\theta_{\mathrm{v}}\right)$ is approximate equal to $\theta_{\mathrm{v}}$.

$$
\begin{align*}
& \sin \theta \approx \theta  \tag{2}\\
& \sin \left(\frac{2 \pi}{\lambda} h_{a} \sin \theta_{v}\right) \approx \frac{2 \pi}{\lambda} h_{a} \sin \theta_{v} \tag{3}
\end{align*}
$$

From formula 2 and formula 3, The variation of RF could be described as formula 4:

$$
\begin{equation*}
\Delta R F=20 \log \frac{\sin \left(\frac{2 \pi}{\lambda} h_{a}^{\prime} \sin \theta_{v}\right)}{\sin \left(\frac{2 \pi}{\lambda} h_{a} \sin \theta_{v}\right)} \approx 20 \log \frac{h_{a}^{\prime}}{h_{a}} \tag{4}
\end{equation*}
$$

At last, the variation of RF in far field could be described as formula 5:

$$
\begin{equation*}
\Delta R F \approx 20 \log \frac{h_{a}^{\prime}}{h_{a}} \tag{5}
\end{equation*}
$$

When $h_{a}$ is doubled, $\Delta R F$ is about 6 dB , seen the result in formula 6 :

$$
\begin{equation*}
\Delta R F \approx 20 \log \frac{2 h_{a}}{h_{a}}=20 \log 2 \approx 6 \tag{6}
\end{equation*}
$$

### 2.2.2. Signal Characteristic at Different Altitude

There are two horizontal distances have been defined to calculation in figure $4, r_{1}=1 \mathrm{~km}$ and $\mathrm{r}_{2}=5 \mathrm{~km}$. But in figure 6, it is not just one altitude for $\mathrm{h}=10 \mathrm{~m}$ only, a series of altitude are added to compare, namely $\mathrm{h}=10 \mathrm{~m}, 50 \mathrm{~m}, 100 \mathrm{~m}, 300 \mathrm{~m}, 600 \mathrm{~m}, 1200 \mathrm{~m}$.

Six heights are divided into three groups. group a, b, c for the case of $r_{1}=1 \mathrm{~km}$ and group e, $\mathrm{f}, \mathrm{g}$ for the case of $r_{2}=5 \mathrm{~km}$, respectively. In group a, RF is almost monotonic increasing with the ascending of $h_{a}$. In group b, monotonicity vanished, and the corresponding curve starts to fluctuate, like a " M " shape. In group c , the relationship between RF and $h_{a}$ seems to be changeable, distribution curve produces violent vibration. The similar phenomenon also appears in case of $\mathrm{r}_{2}=5 \mathrm{~km}$. The difference is vibration only appears at the altitude of 1200 m . More regular distribution curves are presented in low altitude.


Fig.6: RF corresponding to $h_{a}$ with different altitude in front of the centre of antenna array with 1 km and 5 km . For the case of $r=1 \mathrm{~km}$, RF is increasing obviously with the ascending of $h_{a}$ at the altitude of 10 m , while RF is increasing slowly at the altitude of 50 m . At the altitude of 100 m , RF is reversed when $\mathrm{h}_{\mathrm{a}}$ surpasses 10 m . When the altitude higher than 300 m , the RF is vibrated, almost no regular presentation. For the case of $\mathrm{r}=5 \mathrm{~km}$, RF is increasing
obviously with the ascending of $h_{a}$ at the altitude of $10 \mathrm{~m}, 30 \mathrm{~m}$, and 100 m . The phenomenon of RF reversed appears at the altitude of 300 m , when the altitude arrives at 1200 m , almost no regular presentation.

### 2.3. Relationship Between $H_{a}$ and Surface

There are two surface modes established in this section, conical surface model and contour plane model. The range of receive position is not just a single point, or a series of points within a line segment. The scope of the study was expanded to a whole area. And this is not plane, but curve surface.

Coverage zone of localizer 7216A system in two kind of surface would be introduced one by one. The transmitter power of 7216A system is set to 20 watts. The minimum acceptable RF level in space is set to -93 dBm.

Conical Surface
Contour Plane


Fig.7: Two kind of cross section models.
In conical surface model, angle of altitude $\left(\theta_{\mathrm{v}}\right)$ between the horizon and inclined plane is main parameter. In contour plane, fly altitude ( $\mathrm{h}_{\mathrm{ffy}}$ ) is main focus. Because of Earth curvature, contour plane is not a flatten plane, it looks like a sphere. Earth curvature error correction was considered in the follow passage.

### 2.3.1. Conical Surface Coverage Responding

The design of mirror synthesis follows conical surface rule. the conical tip is the ground under the center of the localizer antenna array. The coning angle is corresponding to the elevation $\left(\theta_{\mathrm{v}}\right)$. In conical surface, the coverage zone is more regular than that of contour plane. It just changes with elevation and $h_{\mathrm{a}}$.


Fig.8: Conical plane corresponding to $h_{a}$ with a series of $\theta_{\mathrm{v}}$.
Fig.(a) shows coverage zone in $\theta_{\mathrm{v}}=1^{\circ}$ with different $h_{\mathrm{a}}$. Horizontal coordinate (abscissa x -axis) indicates the front of the antenna array and longitudinal coordinates represents the side direction of the antenna array. The maximum zone with $h_{a}=20 \mathrm{~m}$ (red area) placed at the bottom layer, the second one with $h_{a}=10 \mathrm{~m}$ (blue area) was placed on the bottom one, the next one with $h_{a}=2 \mathrm{~m}$ (yellow area) was placed on the blue layer, the minimum coverage zone with $h_{a}=1 \mathrm{~m}$ (cyan area) was placed on the top of the other three layers. The colorful arrow indicates the stacking order. Identical description method is applied to the other three figures, fig.(b), fig.(c) and fig.(d). It can be note that in fig.(c), coverage range of $h_{a}=10 \mathrm{~m}$ (blue one) is larger than that of $h_{a}=20 \mathrm{~m}$ (red one). This order is different to the other three figures.

In figure 8 , there are four $h_{a}(1 \mathrm{~m}, 2 \mathrm{~m}, 10 \mathrm{~m}, 20 \mathrm{~m})$ as well as four $\theta_{\mathrm{v}}\left(1^{\circ}, 2^{\circ}, 3^{\circ}, 6^{\circ}\right)$ in research. In figure a, the coverage zone of $h_{a}=1 m$ (marked in cyan) is less than that of $h_{a}=2 m$ (marked in yellow), the max coverage distance $\left(d_{\text {max }}\right)$ is about 400 km for $h_{a}=1 \mathrm{~m}$ and 800 km for $h_{a}=2 \mathrm{~m}$. So, the $d_{\text {max }}$ of $h_{a}=1 \mathrm{~m}$ is half of $h_{a}=2 m$. Therefore, the coverage area is quarter of the case of $h_{a}=2 m$. The interesting thing is their coverage shapes are almost the same. And follow the rule of equal proportion distribution. When $h_{a}$ arrives at 10 m (marked in blue), the coverage area has been greatly expanded. It is beyond a radius of 1000 km . when $\mathrm{h}_{\mathrm{a}}$ doubled again, ascending to 20 m (marked in red), the corresponding coverage area in front could not be compared directly. It is only observed by back lobe. Also, the coverage distance is approximately two times of $h_{a}=10 \mathrm{~m}$, about 380 km for $h_{a}=20 \mathrm{~m}$ and 200 km for $h_{a}=10 \mathrm{~m}$. In figure b, the proportion with $h_{a}=1 \mathrm{~m}$ and $h_{a}=2 \mathrm{~m}$ is still 1:2, but it can be observed from back lobe of $h_{a}=10 \mathrm{~m}$ and $h_{a}=20 \mathrm{~m}$, about 400 km for $h_{a}=10 \mathrm{~m}$ and 500 km for $h_{\mathrm{a}}=20 \mathrm{~m}$. Obviously, the ratio is no longer follows 1:2. In figure c , for $\theta_{\mathrm{v}}=3^{\circ}, d_{\max }$ of $h_{a}=10 \mathrm{~m}$ is dramatically more than that of $h_{a}=20 \mathrm{~m}$. However, $d_{\max }$ of $h_{a}=1 \mathrm{~m}$ and $h_{a}=2 m$ is still follows the rule of $1: 2$. In figure $d$, the coverage area of $h_{a}=20 m$ is larger than $h_{a}=10$ once again.

To explain the abnormal phenomenon scientifically, the relative amplitude of mirror synthesis signal corresponding to $\theta_{\mathrm{v}}$ of each $\mathrm{h}_{\mathrm{a}}$ has been drawn in figure 9. For lower $\mathrm{h}_{\mathrm{a}}$, the corresponding curves are almost straight line, but for higher $h_{a}$, their curves begin to bend. For $h_{a}=20 \mathrm{~m}$, the maximum value appears at $\theta_{\mathrm{v}}=$ $2^{\circ}$, and then sharply drops. At $\theta_{v}=3^{\circ}$, the value of $h_{a}=20 \mathrm{~m}$ is less than that of $h_{a}=10 \mathrm{~m}$. this is the reason in figure 8(c), the coverage area is smaller for $h_{a}=20 \mathrm{~m}$. Because of the linear behavior in low $h_{a}$, shape of coverage area keeps good proportion, despite of $\theta_{\mathrm{v}}$ up to $6^{\circ}$.


Fig.9: Relative amplitude corresponding to $\theta_{\mathrm{v}}$ with different $h_{\mathrm{a}}$.
$A=100 \%$ represents the maximum value of each $h_{a}$. When $\theta_{v}$ greater than $2^{\circ}, A\left(h_{a}=20 m\right)$ starts to decline, but $A\left(h_{a}=\right.$ 10 m ) is still ascending. This is the reason coverage range of $h_{a}=10 \mathrm{~m}$ is larger than $h_{a}=20 \mathrm{~m}$ at $\theta_{\mathrm{v}}=3^{\circ}$. When $\theta_{\mathrm{v}}$ arrives at $4^{\circ}$, relative amplitude of $h_{a}=20 \mathrm{~m}$ is negligible. $A\left(h_{a}=20 \mathrm{~m}\right)$ is the minimum value in all height of $h_{a}$ at $4^{\circ}$.

### 2.3.2. Contour Plane Coverage Responding

When the aircraft flies in sky with a certain altitude, the orbit in space is a contour plane. The contour plane is just like the surface of a sphere instead of a flat surface in fact. So, the precise position on the contour plane should be revised for Cartesian coordinates of antenna system ${ }^{[16]}$. The calculation discussed below is based on the hypothesis that the Earth is a spheroidal ball with smooth surface.

In table 3, both of the coverage of plane and contour plane are calculated, and the ratio of $\mathrm{d}_{\text {max }}$ by two circumstances is also listed. It can be found clearly that unrevised model, $\mathrm{d}_{\text {max }}$ of flat surface owns longer distance. For conventional coverage requirement (minimum $\mathrm{RF}=-93 \mathrm{dBm}$ ), $\mathrm{d}_{\text {max }}$ is 147 km for $\mathrm{h}_{\mathrm{fly}}=300$. While the value of revised model is just 64 km . So, it is necessary to revise Earth curvature error. Otherwise, the error is pretty unbelievable.

The ratio of $\mathrm{d}_{\text {max }}$ of different $\mathrm{h}_{\text {fly }}$ is stable, which is always 2.3 for minimum $\mathrm{RF}=-93 \mathrm{dBm}$. In further, the stricter coverage requirements (minimum $\mathrm{RF}=-88 \mathrm{dBm},-83 \mathrm{dBm},-78 \mathrm{dBm},-73 \mathrm{dBm}$ ) were also analyzed. The ratio descents a bit. The higher requirement corresponds the smaller ratio. The error is just $20 \%$ for minimum $\mathrm{RF}=-73 \mathrm{dBm}$. Otherwise, if the coverage requirement was lower standards, the error
would not be negligible, the error correction is necessary. The discussion below, the common coverage requirements (minimum $\mathrm{RF}=-93 \mathrm{Bm}$ ) is always used.

Table 3: Maximum coverage distance ( $\mathrm{d}_{\max }$ ) before and after Earth curvature error correction

| cut off RF $(\mathrm{dBm})$ <br> $\mathrm{h}_{\text {fly }}(\mathrm{m})$ | -93 | -88 | -83 | -78 | -73 |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |
| 300 | $\mathrm{~d}_{\text {max }}(\mathrm{km})$-unrevised (Before) |  |  |  |  |
| 600 | 147 | 110 | 81 | 62 | 46 |
| 1200 | 208 | 155 | 117 | 88 | 65 |
| 2400 | 294 | 221 | 166 | 124 | 93 |
|  | 417 | 312 | 234 | 175 | 131 |
| 300 | $\mathrm{~d}_{\text {max }}(\mathrm{km})$-revised (After) |  |  |  |  |
| 600 | 64 | 59 | 53 | 46 | 39 |
| 1200 | 90 | 84 | 76 | 66 | 55 |
| 2400 | 128 | 119 | 107 | 92 | 78 |
|  | 181 | 169 | 152 | 132 | 110 |
| 300 | ratio of $\mathrm{d}_{\text {max }}$ (Before/After) |  |  |  |  |
| 600 | 2.3 | 1.9 | 1.5 | 1.3 | 1.2 |
| 1200 | 2.3 | 1.8 | 1.5 | 1.3 | 1.2 |
| 2400 | 2.3 | 1.9 | 1.6 | 1.3 | 1.2 |

In general, the minimum RF of signal coverage is -93 dBm , to study more systemically, the coverage requirement was raised. From five kind of coverage requirements (cut off $\mathrm{RF}=-93 \mathrm{dBm},-88 \mathrm{dBm},-83 \mathrm{dBm}$, $-78 \mathrm{dBm},-73 \mathrm{dBm}$ ), the ratio of $\mathrm{d}_{\text {max }}$ (the value of $\mathrm{d}_{\max }$ unrevised divided by the revised one) can be apparently understanding. If Earth curvature unrevised, the contour plane was regarded as flattened, the lower coverage requirement would cause greater error.

In figure 10 , there are three $\mathrm{h}_{\text {fly }}(100 \mathrm{~m}, 600 \mathrm{~m}, 3000 \mathrm{~m})$ as well as four $h_{\mathrm{a}}(1 \mathrm{~m}, 2 \mathrm{~m}, 10 \mathrm{~m}, 20 \mathrm{~m})$ in research. In figure a, scanned with a radius of 50 km , as expected, the higher $h_{a}$ owns the larger coverage area. But the lower $h_{\mathrm{a}}$ owns a sharp lobe in front. in figure $b$, almost shows a same rule. the higher $h_{\text {fly }}$ corresponding larger coverage area. However, in figure $c$, although $d_{\text {max }}$ of $h_{a}=20 \mathrm{~m}$ (red one) is more than $h_{a}=10$ (blue one), there are some gaps in the center.


Fig.10: Contour plane corresponding to $h_{a}$ in different $h_{\text {fly }}$.
Fig.(a) shows coverage zone in the altitude of $h_{\text {fly }}=100 \mathrm{~m}$ with different $h_{a}$. The maximum zone with $h_{d}=20 \mathrm{~m}$ (red area) placed at the bottom layer, the second one with $h_{a}=10 \mathrm{~m}$ (blue area) was placed on the bottom one, the next one with
$h_{a}=2 \mathrm{~m}$ (yellow area) was placed on the blue layer, the minimum coverage zone with $h_{\mathrm{a}}=1 \mathrm{~m}$ (cyan area) was placed on the top of the other three layers. The colorful arrow indicates the stacking order. Identical expression is applied to the other three figures, fig.(b), fig.(c) and fig.(d). It can be note that in fig.(d), the coverage range of $h_{a}=20 \mathrm{~m}$ (red one) is larger than that of $h_{a}=10 \mathrm{~m}$ (blue one). But in fig.(c), red one covered less than blue one within the of radius 50 km .

To find the details more clearly, the case of $\mathrm{h}_{\mathrm{fly}}=3000 \mathrm{~m}$ has been specifically listed in figure 11. For lower $h_{a}$, there is no obvious evidence, seen in the enlarged zone of figure a and figure b. For higher $h_{a}$, both figure c and figure d appear some circles. Because of overlap in figure 10, this coverage insufficient was not discovery systemically. The abnormal zone should be enlarged more detailly.


Fig.11: Contour plane in the altitude of $\mathrm{h}_{\mathrm{fly}}=3 \mathrm{~km}$ with various $\mathrm{h}_{\mathrm{a}}$.
The main graph owns the radius with 220 km . Their insets show the enlarged zone of the center. Each coverage zone of inset covers the area with the radius of 50 km . Circle appears more frequently with the higher $h_{a}$.

### 2.3.2.1. Coverage Insufficient----Headspace Blind Area

To more carefully and intensively, the coverage area of figure 11 is enlarged 100 time. A series of $h_{a}$ with a radius of 5 km can be found clearly in figure 12. All the cases, no matter how high or how low of $\mathrm{h}_{\mathrm{a}}$. exist coverage insufficient, this position is located in the headspace of antenna array. So, it can be called "headspace blind area". In detail, the blind area is comparatively fixed. They are distributed on both sides of the center point. The double holes are related to the vertical pattern of LPDA. The hyperbolic shape originates from twenty antennas array effect.


Fig.12: Contour plane in the altitude of $\mathrm{h}_{\text {fly }}=3 \mathrm{~km}$ with various $\mathrm{h}_{\mathrm{d}}$.
Besides the circle effect, there are some certain zone uncovered. They are located in the position above the headspace of antenna array for all height of $h_{a}$.

### 2.3.2.2. Near Field Situation----Circle Effect

There is not remarkable circle for the cases of $h_{a}$ lower than 5 m . But there are more than two circles for the case of $h_{a}$ higher than 5 m . A lot of circles appear in near field for $h_{a}=20 \mathrm{~m}$. Back to figure 3, these circles are corresponding to the gap of lobes. For lower $h_{a}$, circle in near field would not impact approaching. There are several kilometer distances between localizer antenna array and the threshold of runway. But it is hard to say for higher $h_{a}$.

## 3. Summary

The mirror signal synthesis of localizer antenna array was investigated in series. The heights of localizer antenna ( $h_{a}=1 \mathrm{~m}, 2 \mathrm{~m}, 3 \mathrm{~m}, 4 \mathrm{~m}, 5 \mathrm{~m}, 10 \mathrm{~m}, 15 \mathrm{~m}, 20 \mathrm{~m}$ ) corresponding to radiated space signal were study for both vertical section and 3D surface. From vertical section, the space RF level increase obviously with the ascending of $h_{a}$ below altitude of 50 m . But it is not fitted to high altitude, the signal strength shakes up and down with the ascending of $h_{a}$ above altitude of 600 m . The optimized height of $h_{a}$ is about 4 m obtained from curve fitting. From 3D surface, there were four elevate angle ( $\theta_{\mathrm{v}}=1^{\circ}, 2^{\circ}, 3^{\circ}, 6^{\circ}$ ) in conical surface and three height ( $h_{\text {fly }}=100 \mathrm{~m}, 600 \mathrm{~m}, 3000 \mathrm{~m}$ ) in contour plane have been studied. For conical model, the shape of coverage area of lower $h_{a}$ became equally amplify with the increasing of $\theta_{\mathrm{v}}$. However, it was not monotonically increasing for higher $\mathrm{h}_{\mathrm{a}}\left(\mathrm{h}_{\mathrm{a}}=20 \mathrm{~m}\right)$. For contour plane model, the higher for $\mathrm{h}_{\mathrm{fly}}$, the more area could be covered, especially for higher $h_{a}$, but coverage insufficient also generated, such as headspace blind area and circle effect. Similarly, the 3D model also indicated the $h_{a}$ is not the higher the better. This study can be widely applied to on-site installation of equipment about antenna height demand.

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